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• The linear-phase FIR filter obtained by minimizing the peak absolute value of

 $\varepsilon = \max_{\omega \in \mathbf{R}} \left| E(\omega) \right|$ 

which is usually called the equiripple FIR filter

• After  $\varepsilon$  is minimized, the weighted error function  $|E(\omega)|$  exhibits an equiripple behavior in the frequency range *R* 



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### 1. Design of Equiripple Linear-Phase FIR Filters

• The general form of frequency response of a causal linear-phase FIR filter of length 2*M*+1:

 $H(e^{j\omega}) = e^{-jN\omega/2} e^{j\beta} \breve{H}(\omega)$ 

where the amplitude response  $\breve{H}(\omega)$  is a real function of  $\omega$ 

• Weighted error function is given by  $E(\omega) = W(\omega) \left[ \vec{H}(\omega) - D(\omega) \right]$ 

where  $D(\omega)$  is the desired amplitude response and  $W(\omega)$  is a positive weighting function

### 1. Design of Equiripple Linear-Phase FIR Filters



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#### **Parks-McClellan Algorithm**

- Based on iteratively adjusting the coefficients of  $\breve{H}(\omega)$  until the peak absolute value of  $E(\omega)$  is minimized
- If peak absolute value of  $E(\omega)$  in a band  $\omega_a \le \omega \le \omega_b$  is  $\varepsilon_0$ , then the absolute error satisfies

$$\left| \breve{H}(\omega) - D(\omega) \right| \leq \frac{\varepsilon_0}{\left| W(\omega) \right|}, \ \omega_a \leq \omega \leq \omega_b$$

# 1. Design of Equiripple Linear-Phase FIR Filters

• Thus, weighting function can be chosen either as  $W(\omega) = \begin{cases} 1, & \text{in the passband} \\ \delta_p / \delta_s, & \text{in the stopband} \end{cases}$ or  $W(\omega) = \begin{cases} \delta_s / \delta_p, & \text{in the passband} \\ 1, & \text{in the stopband} \end{cases}$ 

# 1. Design of Equiripple Linear-Phase FIR Filters

- For filter design,
  D(ω) = {1, in the passband 0, in the stopband
   H(ω) is required to satisfy the above desired
- $H(\omega)$  is required to satisfy the above desired response with a ripple of  $\pm \delta_p$  in the passband and a ripple of  $\delta_s$  in the stopband

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