RSC Advances



PAPER



Cite this: RSC Adv., 2015, 5, 11825

Received 3rd December 2014 Accepted 12th January 2015

DOI: 10.1039/c4ra15699d

www.rsc.org/advances

A new high-pressure polymeric nitrogen phase in potassium azide†

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To explore new stable polymeric nitrogen phases in alkali metal azides, the crystalline structures of potassium azide KN₃, are systematically investigated up to 400 GPa by using unbiased structure searching methods combined with first principles density functional calculations. Two high-pressure phases of KN₃, insulator C2/m phase with N³⁻ anions and metallic P6/mmm phase with "N₆" rings were uncovered above 20 GPa and 41 GPa, respectively, which are consistent with recent theoretical works. Above 274 GPa, a stable C2/m-N phase featuring polymerized N is identified for the first time and it is energetically much superior to the previously proposed C2/m-II structure. This C2/m-N structure consists of zig-zag N polymer nets which can be naturally viewed as the polymerization of "N₆" molecules rings in the low-pressure P6/mmm phase under increasing pressure. Furthermore, the structure evolutions and accompanied chemical bonding behavior of KN₃ under pressure are also discussed.

Introduction

Recently, the search for the nonmolecular single-bonded (polymeric) form of solid nitrogen, a typical energy-rich material, has attracted much attention in fundamental science and technological applications. It is known that the polymerization of nitrogen may form a high-energy-density material because the transformation from the weak N-N single bond to extremely strong N≡N triple bond is accompanied by a large energy release (six-fold energy difference, the average bond strength of the N-N single bond is 160 kJ mol⁻¹ and that of the triple bond is 954 kJ mol⁻¹), as a consequence of the thermodynamic stability of the product N2 molecule. The application of high pressure to condensed phases opens an effective route to stabilization of polymeric nitrogen, since pressure can significantly alter the electronic bonding state to modify the physical properties. McMahan and Lesar¹ theoretically predicted that, the molecular N2 assumes a monatomic polymeric nitrogen phase (cubic gauche structure, called cg-N) above 60 GPa, which was later confirmed in high-pressure (>110 GPa) and hightemperature (>2000 K) experiments by Eremets et al.2,3 More

Potassium azide KN_3 , another model system with bodycentered tetragonal structure (I4/mcm, Z=2) at ambient condition, its high-pressure behavior has also been the subject of both experimental and theoretical investigations. Raman scattering up to 4.0 GPa (ref. 16) and X-ray diffraction up to 7.0 GPa (ref. 17) indicate that no phase transition is found in KN_3 these measured pressures. Recent experimental works 7,8 have revealed that a first-order phase transition starts at 13.6 GPa and completes at 32.2 GPa in KN_3 under high pressure. Subsequently, two independent theoretical works performed by Li

recently, alkali metal azides, constructed by spherical cations and linear molecular N₃ anions (a straight chain of three nitrogen atoms linked essentially with double N=N bonds), have been proposed to be suitable precursors in the formation of polymeric nitrogen. It could be expected that the N₃⁻ anion will create polymeric single-covalent-bond networks more easily than diatomic nitrogen, since the N₃⁻ anion is more weakly bonded than the diatomic triple-bonded nitrogen.4 Experimentally, the high-pressure structures and N₃⁻ anion evolution behavior in alkali metal azides LiN₃,⁵ NaN₃,^{4,6} KN₃,^{7,8} RbN₃,⁹ and CsN₃ (ref. 10) have been investigated up to 60 GPa, 160 GPa, 55 GPa, 42 GPa, and 55.4 GPa, respectively. In contrast to other azides, the N₃⁻ anions in NaN₃ were found to transform to a non-molecular nitrogen state with an amorphous-like structure when compressed to 120-160 GPa.4 Theoretically, previous calculations have predicted the polymerization of nitrogen in LiN₃, 11-13 NaN₃, 14 and CsN₃ (ref. 15) to complement experiments. In our previous works, the N_3^- anions in LiN₃ (ref. 12) and NaN₃ (ref. 14) will all transform to "N₆" molecular clusters and then to a polymerized nitrogen phase above 375 GPa and 152 GPa, respectively.

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[†] Electronic supplementary information (ESI) available: See DOI: 10.1039/c4ra15699d

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et al. 18 and Zhang et al. 19 have reported that the ambient I4/mcm structure of KN₃ first transforms to a monoclinic C2/m phase above 20 GPa and then to a metallic hexagonal P6/mmm phase above 40 GPa. Moreover, Li et al. 18 pointed out that the P6/mmm phase of KN₃ further transform into a polymerized nitrogen structure (named as C2/m-II phase) above 296.8 GPa. Although this novel polymerized nitrogen C2/m-II structures proposed, the quest for new energetically stable or metastable polymerized nitrogen structures for KN₃ is still fascinating in view of the wide stable pressure range of P6/mmm phase (40-296.8 GPa). For this purpose, we here present extensive structure searches to uncover the most energetically stable KN₃ phase up to 400 GPa by means of an Crystal structure AnaLYsis by Particle Swarm Optimization algorithm (CALYPSO)^{20,21} in combination with first-principles density functional calculations. This method has been successfully applied to several structures which have been confirmed by independent experiments,22-24 including the high-pressure experimental structure (HP-I phase) of NaN3.14 Indeed, a new polymerized nitrogen phase (C2/m, Z = 4, hereafter denoted asC2/m-N) is uncovered above 274 GPa, which is energetically much superior to the recent reported candidate C2/m-II phase. This new polymeric phase consists of zig-zag N polymer nets which can be naturally viewed as the polymerization of "N6" molecules rings in the low-pressure P6/mmm phase under increasing pressure. The structure evolutions and accompanied chemical bonding behavior of KN3 under pressures are also discussed, and these results provide an insight into the formation of polymeric nitrogen in metal azides.

Computational methods

We performed variable-cell high-pressure structure predictions in the range of 0, 25, 50, 100, 200, 300, and 400 GPa with systems containing one to four formula units (f.u.) in simulation cell through CALYPSO code. 20,21 The effectiveness of our method has been demonstrated by recent successes in predicting highpressure structures of various systems, ranging from elements to binary and ternary compounds.25-30 The underlying local structural relaxations were performed using the VASP31,32 code in the framework of density functional theory³³ with the generalized-gradient approximation (GGA) proposed by Perdew-Burke-Ernzerhof (PBE) exchange-correlation functional.³⁴ The electron and core interactions were included by using the frozencore all-electron projector augmented wave (PAW) method35 with N: 2s²2p³ and K: 3s²3p⁶4s¹ treated as the valence electrons. Tests of the computational parameters showed that energy calculations are well converged to better than 1 meV per atom with a plane-wave energy cutoff of 520 eV and a proper Monkhorst-Pack k meshes³⁶ (4 × 15 × 8 for C2/m-N, 6 × 18 × 7 for C2/m-II, $8 \times 8 \times 15$ for P6/mmm, $14 \times 14 \times 17$ for C2/m, and 10×10^{-2} 10×10 for I4/mcm) in the Brillouin zone. During the geometrical optimization, all forces on atoms were converged to less than 0.001 eV Å^{-1} and the total stress tensor was reduced to the order of 0.01 GPa. The charge density topology was analyzed based on Bader's quantum theory of Atoms-In-Molecules (AIM).37 The phonon calculations were carried out by using a finite displacement approach through the PHONOPY program.³⁸

Results and discussion

At ambient pressure, the ground-state of KN3 revealed by our ab initio structural search is exactly the experimental I4/mcm structure, validating our method adopted here. For high pressures at 25 GPa and 50-200 GPa, our structure searches uncover the most stable structures to be monoclinic C2/m phase and hexagonal P6/mmm phase, respectively, which are consistent with the recent theoretical works. 18,19 Strikingly, the crystal structure and atomic arrangements in this P6/mmm phase (Fig. 1(a)) of KN₃ is similar to the high-pressure P6/m phases found in LiN₃ (ref. 11) and NaN₃ (ref. 14) in our previous works. However, as the P6/m space group indicates, the benzene-like six-membered "N₆" rings layers (Fig. 1(b)) and the P6/mmm Li(Na) sublattice are not in registry. With increasing pressures of 300 GPa and 400 GPa, a promising monoclinic C2/m-N phase including partial single N-N bonds was identified for KN3. Meanwhile, the recent proposed monoclinic C2/m-II phase¹⁸ (as shown in Fig. 1(c)) was also explored as a metastable phase with respect to the C2/m-N phase. Fig. 1(d) shows crystal structure of C2/m-N-KN₃, in which the N atoms adopts a 3D packing consisting of intriguing helical tunnels connected to each other by N-N bonds along the b-axis. The structural details of the lattice parameters and the atomic positions of C2/m-N-KN3 are listed in Table 1 together with available theoretical results for P6/mmm-KN3 and C2/m-II-KN3 at different pressures. Inspection further reveals that both N1 and N2 form three covalent bonds with three neighbors and each N3 atom bonding with two neighbors in C2/m-N-KN3. In this N atoms helical tunnels presented in Fig. 1(e), the bond lengths of two N neighbors are $d_{\text{N1-N2}} = 1.351 \text{ Å}$, $d_{\text{N1-N3}} = 1.267 \text{ Å}$, and $d_{\rm N2-N3}=1.281$ Å at 350 GPa, which are close to the three N-N

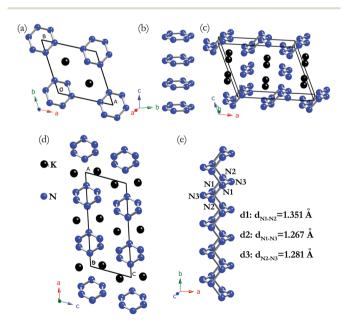


Fig. 1 Crystal structure of P6/mmm-KN $_3$ (a), 2D benzene-like "N $_6$ " ring layers along c-axis in P6/mmm-KN $_3$ (b), crystal structure of C2/m-II-KN $_3$ (c), crystal structure of C2/m-N-KN $_3$ (d), and 3D "N $_6$ " rings along b-axis in C2/m-N-KN $_3$ (e). The black and blue spheres represent K and N atoms, respectively.

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Table 1 Optimized structural parameters of P6/mmm phase at 100 GPa, C2/m-N and C2/m-II phases at 350 GPa

Phase	Source	Pressure (GPa)	Lattice parameters (Å, °)	Atomic coordinates (fractional)
P6/mmm	This work	100	a = b = 5.434, c = 2.396	K 2d (0.6667, 0.3333, 0.5)
			$lpha=eta=90,\gamma=120$	N 6j (0.0000, 0.2370, 0.0)
	Ref. 19	100	a = b = 5.376, c = 2.366	K 2d (0.6667, 0.3333, 0.5)
			$lpha=eta=90,\gamma=120$	N 6j (0.0000, 0.2396, 0.0)
	Ref. 18	150	a = b = 5.202, c = 2.259	K 2d (0.6667, 0.3333, 0.5)
			$lpha=eta=90,\gamma=120$	N 6j (0.0000, 0.2440, 0.0)
C2/m-N	This work	350	a = 9.654, b = 2.177, c = 4.326	K 4m (0.4556, 0.0, 0.7084)
			$lpha=eta=90,\gamma=108.406$	N1 4m (0.8262, 0.0, 0.2652)
				N2 4m (0.2441, 0.0, 0.2697)
				N3 4m (0.8588, 0.0, 0.0035)
C2/m-II	This work	350	a = 7.603, b = 2.120, c = 5.834	K 4i (0.0621, 1.0, 0.7066)
			$lpha=eta=90,\gamma=112.340$	N1 4i (0.1798, 0.0, 0.0977)
				N2 4i (0.9115, 0.5, 0.8975)
				N3 4i (0.2056, 0.5, 0.5)
	Ref. 18	350	a = 7.365, b = 2.092, c = 5.713	K 4i (0.061, 1.0, 0.706)
			$lpha=eta=90,\gamma=111.977$	N1 4 <i>i</i> (0.183, 0.0, 0.097)
				N2 4 <i>i</i> (0.911, 0.5, 0.895)
				N3 4i (0.203, 0.5, 0.5)

bond lengths ($d=1.328\,\text{Å}$, $1.259\,\text{Å}$, and $1.297\,\text{Å}$) reported in high-pressure polymeric $P2_12_12_1$ structure of nitrogen³⁹ at same pressure. The dynamical stability of a crystalline structure requires the eigen frequencies of its lattice vibrations be real for all wavevectors in the whole Brillouin zone. We have thus performed the calculations on the phonon dispersion curves of C2/m-N-KN₃ at 350 GPa. As shown in Fig. 3(a), no imaginary phonon frequency was detected in the whole Brillouin zone for C2/m-N phase, indicating its dynamical stability at high pressure.

To determine the phase transition pressure of KN₃, the enthalpies of the most predicted energetically stable structures are compared over the studied pressure range as shown in Fig. 2. Fig. 2(a) presents the enthalpy differences of the predicted monoclinic C2/m phase and hexagonal P6/mmm phase of KN₃ with respect to the ambient-pressure I4/mcm phase as a function of pressure up to 60 GPa. It is confirmed that the predicted C2/mphase structure becomes more stable than the I4/mcm structure above 20 GPa and is enthalpically stable up to about 41 GPa, above which it transforms to the P6/mmm structure. These two calculated pressure points for $I4/mcm \rightarrow C2/m$ and $C2/m \rightarrow P6/mmm$ structural phase transitions are in excellent agreement with the recent theoretical works. 18,19 Meanwhile, the dependence of volume on pressure is shown in the inset of Fig. 2(a). The results suggest that both $I4/mcm \rightarrow C2/m$ and $C2/m \rightarrow P6/mmm$ phase transitions are first-order with volume drops of 1.8% and 8.9%, which can be easily detected in further experiments. Fig. 2(b) shows the enthalpy curves of our new predicted polymerized nitrogen C2/m-N phase relative to the P6/mmm phase, and the previous reported C2/m-II phase was also considered for comparison. It can be seen that C2/m-N-KN₃ becomes more stable than the P6/mmm-KN₃ above 274 GPa. Compared to the C2/m-N-KN3, the C2/m-II-KN3 possesses larger enthalpy values in the studied pressure ranges from 200 GPa to 500 GPa and thus appear to be a metastable phase. In addition, the thermodynamic stability of C2/m-N-KN₃ at concerned pressure range (100-500 GPa) was examined in terms of the formation enthalpies of the reaction route:

 $\Delta H_{\mathrm{f}} = H_{\mathrm{KN_3}} - H_{\mathrm{K}} - \frac{3}{2} H_{\mathrm{N_2}}$, where the <code>dhcp-K^{40}</code> and <code>Pba2-N_2</code> (ref. 39) were chosen as the reference phases. The calculated formation enthalpies indicate that the formation of the KN3 is exothermic at the studied pressure range. Thus the KN₃ crystal keeps stable against decomposition into the mixture of $K + N_2$. The calculated P-V curves (the inset of Fig. 2(b)) of these two highpressure structures suggested that the phase transitions of $P6/mmm \rightarrow C2/m$ -N is also first-order with volume reduction of 4.2%. The remarkable reconstitution of nitrogen networks in $P6/mmm \rightarrow C2/m$ -N phase transition can naturally explained the pressure effect on the polymerization of nitrogen in KN₃. As shown in Fig. 1(a) and (b), the six N atoms within the P6/mmm phase form a benzene-like "N6" ring layers, K and N layers are localized in different layers and construct an intriguing N-K-N sandwiches structure. With increasing pressure above 274 GPa, the planar "N₆" rings in low-pressure P6/mmm phase were strongly distorted and formed a dense 3D puckered "N₆" rings network connected by N1-N2 bonds (see Fig. 1(e)) with concomitant displacement of K atoms in high-pressure C2/m-N phase. While the dimensionality of the nitrogen covalent bond network in KN₃ from 2D to 3D as pressure increases, there is a trend of decreasing local symmetry of nitrogen atoms in the structural sequence $P6/mmm \rightarrow C2/m-N$. These results may provide value implications for the formation of polymeric nitrogen in other metal azides.

The rearrangement of atoms is always accompanied by a notable change of properties for solids, especially for electronic properties. To explore that, we have calculated the total and site projected density of states (DOS), band structure, and Electronic Localization Function (ELF)⁴¹ distributions of P6/mmm-KN₃ and C2/m-N-KN₃ at 100 GPa and 350 GPa, respectively. Consensus have been reached^{18,19} on that both ambient-pressure I4/mcm and high-pressure C2/m structures of KN₃ exhibit insulating characters in their stable pressure range and thus are not shown here. As shown in Fig. 3(b) and (c), the screened hybrid density functional as proposed by Heyd, Scuzeria, and Ernzerhof (HSE06)⁴²

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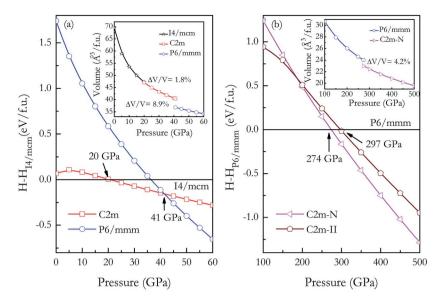


Fig. 2 Enthalpies differences of C2/m-KN₃ and P6/mmm-KN₃ relative to ambient-pressure I4/mcm-KN₃ as a function of pressure (a) and enthalpy differences for C2/m-N-KN₃ relative to P6/mmm-KN₃ as a function of pressure (b).

is employed to investigate the band structures and density of states of P6/mmm-KN $_3$ and C2/m-N-KN $_3$. For P6/mmm-KN $_3$ at 100 GPa in Fig. 3(b), one can see that the HSE06 calculated band structures cross the Fermi level along $\Gamma \to A$, $H \to K$, $M \to L$ directions in the Brillouin zone, indicating its metallic character. However, Fig. 3(c) presents that the C2/m-N-KN $_3$ is a semiconductor

characterized by an indirect band gap of \sim 1.59 eV. Therefore, the pressure-induced phase transition sequences of $C2/m \rightarrow P6/mmm$ and $P6/mmm \rightarrow C2/m$ -N for KN₃ are accompanied by metal-semiconductor transitions, first from insulating to metallic state at 41 GPa and then from metallic back to semiconducting state at 274 GPa. This unusual change of the electronic structure of KN₃

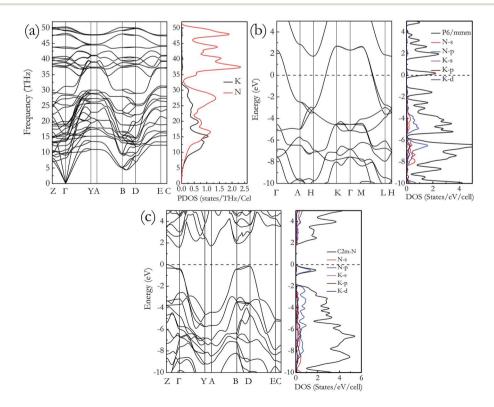


Fig. 3 Phonon dispersion curves of C2/m-N-KN₃ at 350 GPa (a), the band structure and density of states of P6/mmm-KN₃ at 100 GPa (b), and the band structure and density of states of C2/m-N-KN₃ at 350 GPa (c). The horizontal dashed lines denote the Fermi level.

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under pressure is similar to that found in LiN3.12 The atomresolved DOS of P6/mmm and C2/m-N structures reveal that the densities of states near Fermi levels are mainly originated form the N orbitals electrons. As reported in previous work, 19 the benzenelike "N₆" rings in the P6/mmm-KN₃ indicates that the N atoms are in sp² hybridization and each N atom forms two σ bonds with two neighboring N atoms. The extra sp² orbitals are also filled and form the lone pairs, as shown in Fig. 4(a). We found through Bader charge analysis that the charge transfer from K to N atom is 0.76e in one f.u., signifying the K-N ionic bonding nature. This means that the N_6^{2-} anion in P6/mmm phase has nearly 8 π -electrons. Six P_{τ} orbitals form three π bonding orbitals and three π antibonding orbitals. Thus, the π antibonding orbitals are partially occupied by two electrons, accompanied by two conduction bands crossing the Fermi level as shown in Fig. 3(b). In the 3D puckered "N₆" rings network of C2/m-N-KN₃ shown in Fig. 1(e), all N1 and N2 atoms are in the sp³ hybridization and form three N-N σ bonds with neighboring N atoms and one lone pair. The N3 atoms in this puckered rings form two N–N σ bonds with neighboring N atoms and two lone pairs. The strong covalent bondings between different inequivalent N atoms as well as the lone pairs on the side N atoms are also revealed by the ELF (Fig. 4(b)). Therefore, all the bonding states and lone pair states are filled and all the antibonding states are unoccupied in C2/m-N-KN3, leading to a semiconducting state.

The nature of chemical bonding in P6/mmm-KN₃ and C2/m-N-KN₃ at 100 GPa and 350 GPa were further studied through a topological analysis of charge density using the Bader atoms-in-molecules (AIM) method at HSE06 functionals level. The basic idea of AIM analysis is to extract bonding information from the electron density $\rho(r)$. The analysis of its electron density gradient $\nabla \rho(r)$ helps to define an atom within a molecule or solid through the "zero-flux surface" condition. The analysis of the electron density extrema, *i.e.*, at critical points, located at $r_{\rm CP}$ for which $\nabla \rho(r_{\rm CP})$, allows the characterization of the nature of bonding.⁴³ The (3, -1) bond critical points (BCPs) which

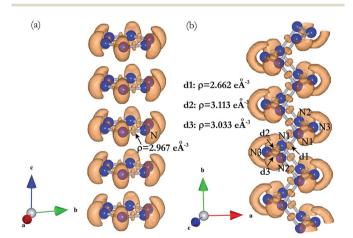


Fig. 4 The ELF distributions of 2D " N_6 " rings along c-axis in P6/mmm-K N_3 (a) and 3D " N_6 " rings along b-axis in C2/m-N-K N_3 . The electron densities located at different (3, -1) bond critical points (BCPs) in 2D " N_6 " rings and 3D " N_6 " rings are also presented.

locate at the adjacent nitrogen atoms ($d_{N-N} = 1.288 \text{ Å}$) within pseudo-benzene "N₆" ring possess negative $\nabla^2 \rho(r_{\rm CP})$ (Laplacian value) and large $\rho(r_{\rm CP})$ (local electronic density of 2.967 eÅ⁻³), indicating the strong double N=N covalent bonding nature. However, $\rho(\overrightarrow{r}_{CP})$ of inter-"N₆" BCPs are much smaller (i.e. 0.263 eÅ-3) and the corresponding $\nabla^2 \rho(\overrightarrow{r}_{CP})$ are positive, suggesting closed shell interaction among these "N₆" rings. For C2/m-N-KN₃ at 350 GPa, both BCPs located between N2-N3 (1.281 Å) and N1-N3 atoms (1.267 Å) exhibit negative $\nabla^2 \rho(\mathbf{r}_{CP})$ and large $\rho(\mathbf{r}_{CP})$ of 3.033 and 3.133 eÅ⁻³, which are little larger than that of adjacent nitrogen atoms within "N6" ring in low-pressure P6/mmm structure. As expected, the BCPs sitting between N1 and N2 atoms have relative smaller value of local density $\rho(\mathbf{r}_{CP})$ (2.662 eÅ⁻³) due to its longer bond length of 1.351 Å, which is consistent with its three-fold coordinated environment. The BCPs of unequivalent N and K atoms in P6/mmm- KN_3 and C2/m-N- KN_3 are all positive, indicating closed shell interaction character which is in agreement with an "ionized" K picture presented in the partial DOS (Fig. 3(b) and (c)).

Conclusions

In summary, an unbiased structure search method in combination with first-principles calculations was employed to explore the high-pressure polymeric nitrogen phase of KN_3 up to 400 GPa. For the first time, we identify a novel monoclinic C2/m-N phase featuring 3D polymerized nitrogen above 274 GPa, and this new polymeric nitrogen phase is energetically much superior to the previously proposed C2/m-II structure. Phonon dispersion and formation enthalpies calculations suggest that C2/m-N is dynamically stable and is stable against the decomposition into the structure mixture of $K+N_2$ at high pressure. The analysis of the electronic structure reveals that the polymerization of nitrogen from 2D " N_6 " molecular rings to 3D puckered " N_6 " rings network in KN_3 is driven by hybridization of N atomic orbitals, which changes from sp^2 to sp^3 under very high pressure.

Acknowledgements

This work was financially supported by the Natural Science Foundation of China (no. 11204007) and Natural Science Basic Research plan in Shaanxi Province of China (grant no. 2012JQ1005).

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