A new high-pressure polymeric nitrogen phase in potassium azide†

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To explore new stable polymeric nitrogen phases in alkali metal azides, the crystalline structures of potassium azide KN₃ are systematically investigated up to 400 GPa by using unbiased structure searching methods combined with first principles density functional calculations. Two high-pressure phases of KN₃, insulator C2/m phase with N₃⁻ anions and metallic P6/mmmm phase with ‘N₆’ rings were uncovered above 20 GPa and 41 GPa, respectively, which are consistent with recent theoretical works. Above 274 GPa, a stable C2/m-N phase featuring polymerized N is identified for the first time and it is energetically much superior to the previously proposed C2/m-Il structure. This C2/m-N structure consists of zig-zag N polymer nets which can be naturally viewed as the polymerization of ‘N₆’ molecules rings in the low-pressure P6/mmmm phase under increasing pressure. Furthermore, the structure evolutions and accompanied chemical bonding behavior of KN₃ under pressure are also discussed.

Introduction

Recently, the search for the nonmolecular single-bonded (polymeric) form of solid nitrogen, a typical energy-rich material, has attracted much attention in fundamental science and technological applications. It is known that the polymerization of nitrogen may form a high-energy-density material because the transformation from the weak N−N single bond to extremely strong N≡N triple bond is accompanied by a large energy release (six-fold energy difference, the average bond strength of the N−N single bond is 160 kJ mol⁻¹ and that of the triple bond is 954 kJ mol⁻¹), as a consequence of the thermodynamic stability of the product N₂ molecule. The application of high pressure to condensed phases opens an effective route to stabilization of polymeric nitrogen, since pressure can significantly alter the electronic bonding state to modify the physical properties. McMahan and Lesar¹ theoretically predicted that, the molecular N₂ assumes a monatomic polymeric nitrogen phase (cubic gauche structure, called cg-N) above 60 GPa, which was later confirmed in high-pressure (>110 GPa) and high-temperature (>2000 K) experiments by Eremets et al.²³ More recently, alkali metal azides, constructed by spherical cations and linear molecular N₃⁻ anions (a straight chain of three nitrogen atoms linked essentially with double N≡N bonds), have been proposed to be suitable precursors in the formation of polymeric nitrogen. It could be expected that the N₃⁻ anion will create polymeric single-covalent-bond networks more easily than diatomic nitrogen, since the N₃⁻ anion is more weakly bonded than the diatomic triple-bonded nitrogen.⁴ Experimentally, the high-pressure structures and N₃⁻ anion evolution behavior in alkali metal azides LiN₃,⁵ NaN₃,⁵⁵ KN₃,⁷,⁸ RbN₃,⁹ and CsN₃ (ref. 10) have been investigated up to 60 GPa, 160 GPa, 55 GPa, 42 GPa, and 55.4 GPa, respectively. In contrast to other azides, the N₃⁻ anions in NaN₃ were found to transform to a non-molecular nitrogen state with an amorphous-like structure when compressed to 120–160 GPa.⁴ Theoretically, previous calculations have predicted the polymerization of nitrogen in LiN₃,⁵⁰–⁵² NaN₃,⁴⁴ and CsN₃ (ref. 15) to complement experiments. In our previous works, the N₃⁻ anions in LiN₃ (ref. 12) and NaN₃ (ref. 14) will all transform to “N₆” molecular clusters and then to a polymerized nitrogen phase above 375 GPa and 152 GPa, respectively.

Potassium azide KN₃, another model system with body-centered tetragonal structure (I4/mcm, Z = 2) at ambient condition, its high-pressure behavior has also been the subject of both experimental and theoretical investigations. Raman scattering up to 4.0 GPa (ref. 16) and X-ray diffraction up to 7.0 GPa (ref. 17) indicate that no phase transition is found in KN₃ these measured pressures. Recent experimental works⁷⁸ have revealed that a first-order phase transition starts at 13.6 GPa and completes at 32.2 GPa in KN₃ under high pressure. Subsequently, two independent theoretical works performed by Li...
et al.\textsuperscript{18} and Zhang et al.\textsuperscript{19} have reported that the ambient \textit{I4/mcm} structure of KN\textsubscript{3} first transforms to a monoclinic \textit{C2/m} phase above 20 GPa and then to a metallic hexagonal \textit{P6/mmm} phase above 40 GPa. Moreover, Li et al.\textsuperscript{18} pointed out that the \textit{P6/mmm} phase of KN\textsubscript{3} further transforms into a polymerized nitrogen structure (named as \textit{C2/m-II} phase) above 296.8 GPa. Although this novel polymerized nitrogen \textit{C2/m-II} structures proposed, the quest for new energetically stable or metastable polymerized nitrogen structures for KN\textsubscript{3} is still fascinating in view of the wide stable pressure range of \textit{P6/mmm} phase (40–296.8 GPa). For this purpose, we here present extensive structure searches to uncover the most energetically stable KN\textsubscript{3} phase up to 400 GPa by means of an Crystal structure AnalYsis by Particle Swarm Optimization algorithm (CALYPSO)\textsuperscript{28,29} in combination with first-principles density functional calculations. This method has been successfully applied to several structures which have been confirmed by independent experiments,\textsuperscript{22–24} including the high-pressure experimental structure (HP-I phase) of NaN\textsubscript{3}\textsuperscript{14} Indeed, a new polymerized nitrogen phase (\textit{C2/m, Z = 4}, hereafter denoted as \textit{C2/m-N}) is uncovered above 274 GPa, which is energetically much superior to the recent reported candidate \textit{C2/m-II} phase. This new polymeric phase consists of zig-zag N polymer nets which can be naturally viewed as the polymerization of “N\textsubscript{6}” molecules rings in the low-pressure \textit{P6/mmm} phase under increasing pressure. The structure evolutions and accompanied chemical bonding behavior of KN\textsubscript{3} under pressures are also discussed, and these results provide an insight into the formation of polymeric nitrogen in metal azides.

Computational methods

We performed variable-cell high-pressure structure predictions in the range of 0, 25, 50, 100, 200, 300, and 400 GPa with systems containing one to four formula units (f.u.) in simulation cell through CALYPSO code.\textsuperscript{20,21} The effectiveness of our method has been demonstrated by recent successes in predicting high-pressure structures of various systems, ranging from elements to binary and ternary compounds.\textsuperscript{25–30} The underlying local structural relaxations were performed using the VASP\textsuperscript{31,32} code in the framework of density functional theory\textsuperscript{23} with the generalized-gradient approximation (GGA) proposed by Perdew–Burke–Ernzerhof (PBE) exchange–correlation functional.\textsuperscript{14} The electron and core interactions were included by using the frozen-core all-electron projector augmented wave (PAW) method\textsuperscript{35} with N: 2s\textsuperscript{2}2p\textsuperscript{3} and K: 3s\textsuperscript{2}3p\textsuperscript{5}4s\textsuperscript{1} treated as the valence electrons. Tests of the computational parameters showed that energy calculations are well converged to better than 1 meV per atom with a plane-wave energy cutoff of 520 eV and a proper Monkhorst–Pack \textit{k} meshes\textsuperscript{46} (4 × 15 × 8 for \textit{C2/m-N}, 6 × 18 × 7 for \textit{C2/m-II}, 8 × 8 × 15 for \textit{P6/mmm}, 14 × 14 × 17 for \textit{C2/m}, and 10 × 10 × 10 for \textit{I4/mcm}) in the Brillouin zone. During the geometrical optimization, all forces on atoms were converged to less than 0.001 eV Å\textsuperscript{-1} and the total stress tensor was reduced to the order of 0.01 GPa. The charge density topology was analyzed based on Bader’s quantum theory of Atoms-In-Molecules (AIM).\textsuperscript{37} The phonon calculations were carried out by using a finite displacement approach through the PHONOPY program.\textsuperscript{38}

Results and discussion

At ambient pressure, the ground-state of KN\textsubscript{3} revealed by our \textit{ab initio} structural search is exactly the experimental \textit{I4/mcm} structure, validating our method adopted here. For high pressures at 25 GPa and 50–200 GPa, our structure searches uncover the most stable structures to be monoclinic \textit{C2/m} phase and hexagonal \textit{P6/mmm} phase, respectively, which are consistent with the recent theoretical works.\textsuperscript{18,19} Strikingly, the crystal structure and atomic arrangements in this \textit{P6/mmm} phase (Fig. 1(a)) of KN\textsubscript{3} is similar to the high-pressure \textit{P6/m} phases found in LiN\textsubscript{3} (ref. 11) and NaN\textsubscript{3} (ref. 14) in our previous works. However, as the \textit{P6/m} space group indicates, the benzene-like six-membered “N\textsubscript{6}” rings layers (Fig. 1(b)) and the \textit{P6/mmm} Li(Na) sublattice are not in registry. With increasing pressures of 300 GPa and 400 GPa, a promising monoclinic \textit{C2/m-N} phase including partial single N–N bonds was identified for KN\textsubscript{3}. Meanwhile, the recent proposed monoclinic \textit{C2/m-II} phase\textsuperscript{18} (as shown in Fig. 1(c)) was also explored as a metastable phase with respect to the \textit{C2/m-N} phase. Fig. 1(d) shows crystal structure of \textit{C2/m-N-KN3}, in which the N atoms adopts a 3D packing consisting of intriguing helical tunnels connected to each other by N–N bonds along the \textit{b}-axis. The structural details of the lattice parameters and the atomic positions of \textit{C2/m-N-KN3} are listed in Table 1 together with available theoretical results for \textit{P6/mmm-KN3} and \textit{C2/m-II-KN3} at different pressures. Inspection further reveals that both N1 and N2 form three covalent bonds with three neighbors and each N3 atom bonding with two neighbors in \textit{C2/m-N-KN3}. In this N atoms helical tunnels presented in Fig. 1(e), the bond lengths of two N neighbors are \textit{d}_{N1-N2} = 1.351 Å, \textit{d}_{N1-N3} = 1.267 Å, and \textit{d}_{N2-N3} = 1.281 Å at 350 GPa, which are close to the three N–N

![Fig. 1. Crystal structure of \textit{P6/mmm-KN3} (a), 2D benzene-like “N\textsubscript{6}” rings layers along c-axis in \textit{P6/mmm-KN3} (b), crystal structure of \textit{C2/m-II-KN3} (c), crystal structure of \textit{C2/m-N-KN3} (d), and 3D “N\textsubscript{6}” rings along b-axis in \textit{C2/m-N-KN3} (e). The black and blue spheres represent K and N atoms, respectively.](image-url)
bond lengths \(d = 1.328 \AA, 1.259 \AA, \text{ and } 1.297 \AA\) reported in high-pressure polymeric \(P2_12_12_1\) structure of nitrogen\(^{19}\) at same pressure. The dynamical stability of a crystalline structure requires the eigen frequencies of its lattice vibrations be real for all wavevectors in the whole Brillouin zone. We have thus performed the calculations on the phonon dispersion curves of \(C2/m-N-KN_3\) at 350 GPa. As shown in Fig. 3(a), no imaginary phonon frequency was detected in the whole Brillouin zone for \(C2/m-N\) phase, indicating its dynamical stability at high pressure.

To determine the phase transition pressure of \(KN_3\), the enthalpies of the most predicted energetically stable structures are compared over the studied pressure range as shown in Fig. 2. Fig. 2(a) presents the enthalpy differences of the predicted monoclinic \(C2/m\) phase and triclinic \(P6/mmm\) phase of \(KN_3\) with respect to the ambient-pressure \(14/mcm\) phase as a function of pressure up to 60 GPa. It is confirmed that the predicted \(C2/m\) phase structure becomes more stable than the \(14/mcm\) structure above 20 GPa and is enthalpically stable up to about 41 GPa, above which it transforms to the \(P6/mmm\) structure. These two calculated pressure points for \(14/mcm \rightarrow C2/m\) and \(C2/m \rightarrow P6/mmm\) structural phase transitions are in excellent agreement with the recent theoretical works.\(^{18,19}\) Meanwhile, the dependence of volume on pressure is shown in the inset of Fig. 2(a). The results suggest that both \(14/mcm \rightarrow C2/m\) and \(C2/m \rightarrow P6/mmm\) phase transitions are first-order with volume drops of 1.8% and 8.9%, which can be easily detected in further experiments. Fig. 2(b) shows the enthalpy curves of our new predicted polymeric nitrogen \(C2/m-N\) phase relative to the \(P6/mmm\) phase, and the previous reported \(C2/m-II\) phase was also considered for comparison. It can be seen that \(C2/m-N-KN_3\) becomes more stable than the \(P6/mmm-KN_3\) above 274 GPa. Compared to the \(C2/m-N-KN_3\), the \(C2/m-II-KN_3\) possesses larger enthalpy values in the studied pressure ranges from 200 GPa to 500 GPa and thus appear to be a metastable phase. In addition, the thermodynamic stability of \(C2/m-N-KN_3\) at concerned pressure range (100–500 GPa) was examined in terms of the formation enthalpies of the reaction route:

\[ \Delta H_f = H_{KN_3} - H_K - \frac{3}{2}H_{N_2} \]

where the \(^{dih}P-KN_3\) and \(^{Pba}N_2\) (ref. 39) were chosen as the reference phases. The calculated formation enthalpies indicate that the formation of the \(KN_3\) is exothermic at the studied pressure range. Thus the \(KN_3\) crystal keeps stable against decomposition into the mixture of \(K + N_2\). The calculated \(P-V\) curves (the inset of Fig. 2(b)) of these two high-pressure structures suggested that the phase transitions of \(P6/mmm \rightarrow C2/m-N\) is also first-order with volume reduction of 4.2%. The remarkable reconstitution of nitrogen networks in \(P6/mmm \rightarrow C2/m-N\) phase transition can naturally explain the pressure effect on the polymerization of nitrogen in \(KN_3\). As shown in Fig. 1(a) and (b), the six \(N_6\) atoms within the \(P6/mmm\) phase form a benzene-like \(“N_6”\) ring layers, \(K\) and \(N\) layers are localized in different layers and construct an intriguing \(N-K-N\) sandwiches structure. With increasing pressure above 274 GPa, the planar \("N_6"\) rings in low-pressure \(P6/mmm\) phase were strongly distorted and formed a dense 3D puckered \("N_6"\) rings network connected by N1–N2 bonds (see Fig. 1(e)) with concomitant displacement of \(K\) atoms in high-pressure \(C2/m-N\) phase. While the dimensionality of the nitrogen covalent bond network in \(KN_3\) from 2D to 3D as pressure increases, there is a trend of decreasing local symmetry of nitrogen atoms in the structural sequence \(P6/mmm \rightarrow C2/m-N\). These results may provide valuable implications for the formation of polymeric nitrogen in other metal azides.

The rearrangement of atoms is always accompanied by a notable change of properties for solids, especially for electronic properties. To explore that, we have calculated the total and site projected density of states (DOS), band structure, and Electronic Localization Function (ELF)\(^{41}\) distributions of \(P6/mmm-KN_3\) and \(C2/m-N-KN_3\) at 100 GPa and 350 GPa, respectively. Consensus have been reached\(^{18,19}\) on that both ambient-pressure \(14/mcm\) and high-pressure \(C2/m\) structures of \(KN_3\) exhibit insulating characters in their stable pressure range and thus are not shown here. As shown in Fig. 3(b) and (c), the screened hybrid density functional as proposed by Heyd, Scuizera, and Ernzerho (HSE06)\(^{42}\)
is employed to investigate the band structures and density of states of \(P6/m\) \(-\) KN\(_3\) and \(C2/m\) \(-\) KN\(_3\). For \(P6/m\) \(-\) KN\(_3\) at 100 GPa in Fig. 3(b), one can see that the HSE06 calculated band structures cross the Fermi level along \(G/A\), \(H/K\), \(M/L\) directions in the Brillouin zone, indicating its metallic character. However, Fig. 3(c) presents that the \(C2/m\) \(-\) KN\(_3\) is a semiconductor characterized by an indirect band gap of ~1.59 eV. Therefore, the pressure-induced phase transition sequences of \(C2/m\) \(\rightarrow\) \(P6/m\) \(\rightarrow\) \(C2/m\) \(-\) KN\(_3\) for KN\(_3\) are accompanied by metal–semiconductor transitions, first from insulating to metallic state at 41 GPa and then from metallic back to semiconducting state at 274 GPa. This unusual change of the electronic structure of KN\(_3\).
under pressure is similar to that found in LiN$_3$\textsuperscript{13}. The atom-resolution DOS of P6/mmm and C2/m-N structures reveal that the densities of states near Fermi levels are mainly originated from the N orbitals electrons. As reported in previous work\textsuperscript{19}, the benzene-like “N$_6$” rings in the P6/mmm-KN$_3$ indicates that the N atoms are in sp$^2$ hybridization and each N atom forms two σ bonds with two neighboring N atoms. The extra sp$^3$ orbitals are also filled and form the lone pairs, as shown in Fig. 4(a). We found through Bader charge analysis that the charge transfer from K to N atom is 0.76e in one f.u., signifying the K–N ionic bonding nature. This means that the N$_6$$^2$– anion in P6/mmm phase has nearly 8 π-electrons. Six P$_2$ orbitals form three π bonding orbitals and three π antibonding orbitals. Thus, the π antibonding orbitals are partially occupied by two electrons, accompanied by two conduction bands crossing the Fermi level as shown in Fig. 3(b). In the 3D puckered “N$_6$” rings network of C2/m-N-KN$_3$, shown in Fig. 1(e), all N1 and N2 atoms are in the sp$^3$ hybridization and form three N–N σ bonds with neighboring N atoms and one lone pair. The N3 atoms in this puckered rings form two N–N σ bonds with neighboring N atoms and two lone pairs. The strong covalent bonding between different inequivalent N atoms as well as the lone pairs on the side N atoms are also revealed by the ELF (Fig. 4(b)). Therefore, all the bonding states and lone pair states are filled and the antibonding states are unoccupied in C2/m-N-KN$_3$, leading to a semiconducting state.

The nature of chemical bonding in P6/mmm-KN$_3$ and C2/m-N-KN$_3$ at 100 GPa and 350 GPa were further studied through a topological analysis of charge density using the Bader atoms-in-molecules (AIM) method at HSE06 functionals level. The basic idea of AIM analysis is to extract bonding information from the electron density $\rho(r)$. The analysis of its electron density gradient $\nabla \rho(r)$ helps to define an atom within a molecule or solid through the “zero-flux surface” condition. The analysis of the electron density extrema, i.e., at critical points, located at $r_{CP}$ for which $\nabla^2 \rho(r_{CP})$, allows the characterization of the nature of bonding.$^{41}$ The (3, −1) bond critical points (BCPs) which locate at the adjacent nitrogen atoms ($d_{K-N} = 1.288$ Å) within pseudo-benzene “N$_6$” ring possess negative $\nabla^2 \rho(r_{CP})$ (Laplacian value) and large $\rho(r_{CP})$ (local electronic density of 2.967 eÅ$^{-3}$), indicating the strong double N=K covalent bonding nature. However, $\rho(r_{CP})$ of inter-“N$_6$” BCPs are much smaller (i.e. 0.263 eÅ$^{-3}$) and the corresponding $\nabla^2 \rho(r_{CP})$ are positive, suggesting closed shell interaction among these “N$_6$” rings. For C2/m-N-KN$_3$ at 350 GPa, both BCPs located between N2–N3 (1.281 Å) and N1–N3 atoms (1.267 Å) exhibit negative $\nabla^2 \rho(r_{CP})$ and large $\rho(r_{CP})$ of 3.034 and 3.133 eÅ$^{-3}$, which are little larger than that of adjacent nitrogen atoms within “N$_6$” ring in low-pressure P6/mmm structure. As expected, the BCPs sitting between N1 and N2 atoms have relative smaller value of local density $\rho(r_{CP})$ (2.662 eÅ$^{-3}$) due to its longer bond length of 1.351 Å, which is consistent with its three-fold coordinated environment. The BCPs of inequivalent N and K atoms in P6/mmm-KN$_3$ and C2/m-N-KN$_3$ are all positive, indicating closed shell interaction which is in agreement with an “ionized” K picture presented in the partial DOS (Fig. 3(b) and (c)).

**Conclusions**

In summary, an unbiased structure search method in combination with first-principles calculations was employed to explore the high-pressure polymeric nitrogen phase of KN$_3$ up to 400 GPa. For the first time, we identify a novel monoclinic C2/m-N phase featuring 3D polymerized nitrogen above 274 GPa, and this new polymeric nitrogen phase is energetically much superior to the previously proposed C2/m-II structure. Phonon dispersion and formation enthalpies calculations suggest that C2/m-N is dynamically stable and is stable against the decomposition into the structure mixture of K + N$_2$ at high pressure. The analysis of the electronic structure reveals that the polymerization of nitrogen from 2D “N$_6$” molecular rings to 3D puckered “N$_6$” rings network in KN$_3$ is driven by hybridization of N atomic orbitals, which changes from sp$^2$ to sp$^3$ under very high pressure.

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**References**
